



a.) Find the induced current at this instant.

Faraday's law: $\mathcal{E} = \left| \frac{d\Phi_m}{dt} \right|$

where:

$$\Phi_m = \int \vec{B} \cdot d\vec{A} \quad \text{as we did in WB 30-4:}$$

$$\Phi_m = \frac{\mu_0 I L}{2\pi} \ln\left(\frac{x+w}{x}\right) = \frac{\mu_0 I L}{2\pi} \{ \ln(x+w) - \ln x \}$$

Now:

$$\frac{d\Phi_m}{dt} = \frac{d\Phi_m}{dx} \frac{dx}{dt} = \frac{\mu_0 I L}{2\pi} \left\{ \frac{1}{x+w} - \frac{1}{x} \right\} v$$

$$= \frac{\mu_0 I L}{2\pi} \left(\frac{-w}{x(x+w)} \right) v$$

or,

$$\frac{d\Phi_m}{dt} = \frac{\mu_0 I L}{2\pi} \frac{d}{dt} \{ \ln(x+w) - \ln x \}$$

$$= \frac{\mu_0 I L}{2\pi} \left\{ \frac{1}{x+w} \frac{dx}{dt} - \frac{1}{x} \frac{dx}{dt} \right\}$$

$$= \frac{\mu_0 I L}{2\pi} \left(\frac{-w}{x(x+w)} \right) v$$

So:

$$\mathcal{E} = \left| \frac{d\Phi_m}{dt} \right| = \frac{\mu_0 I L}{2\pi} \left(\frac{w}{x(x+w)} \right) v$$

and

$$I_{in} = \frac{\mathcal{E}}{R} = \frac{\mu_0 I L}{2\pi R} \left\{ \frac{w}{x(x+w)} \right\} v$$

b.)

also, since the flux is decreasing,

\vec{B}_{in} reinforces \vec{B} from wire

∴ I_{in} is CW.