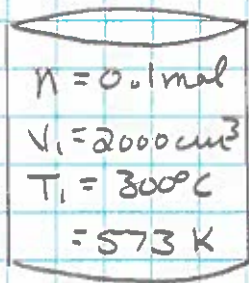
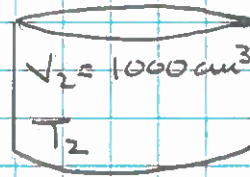
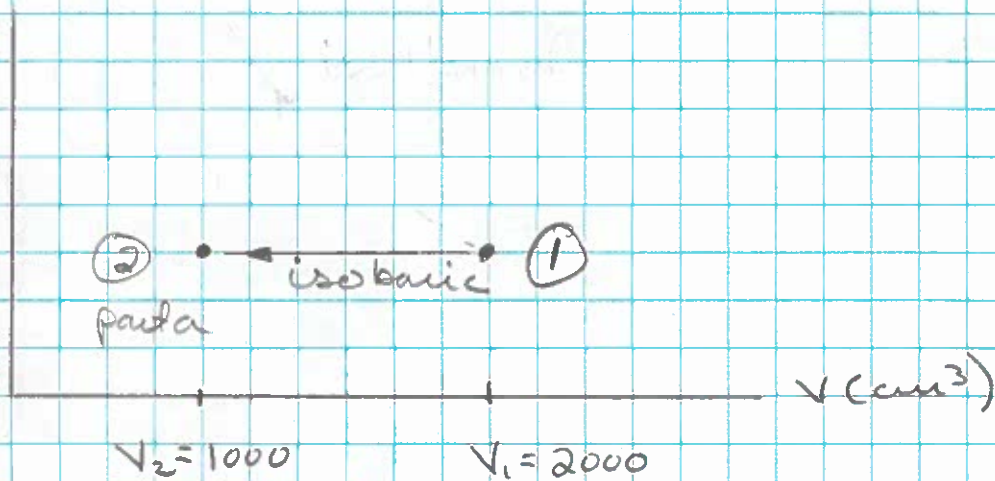


State 1State 2

First, show processes on a PV diagram:

a.) Isobaricb.) Isobaric, $P_2 = P_1$

$$W_{1 \rightarrow 2} = - \int_{V_1}^{V_2} P dV = -(\text{area under isobaric path.})$$

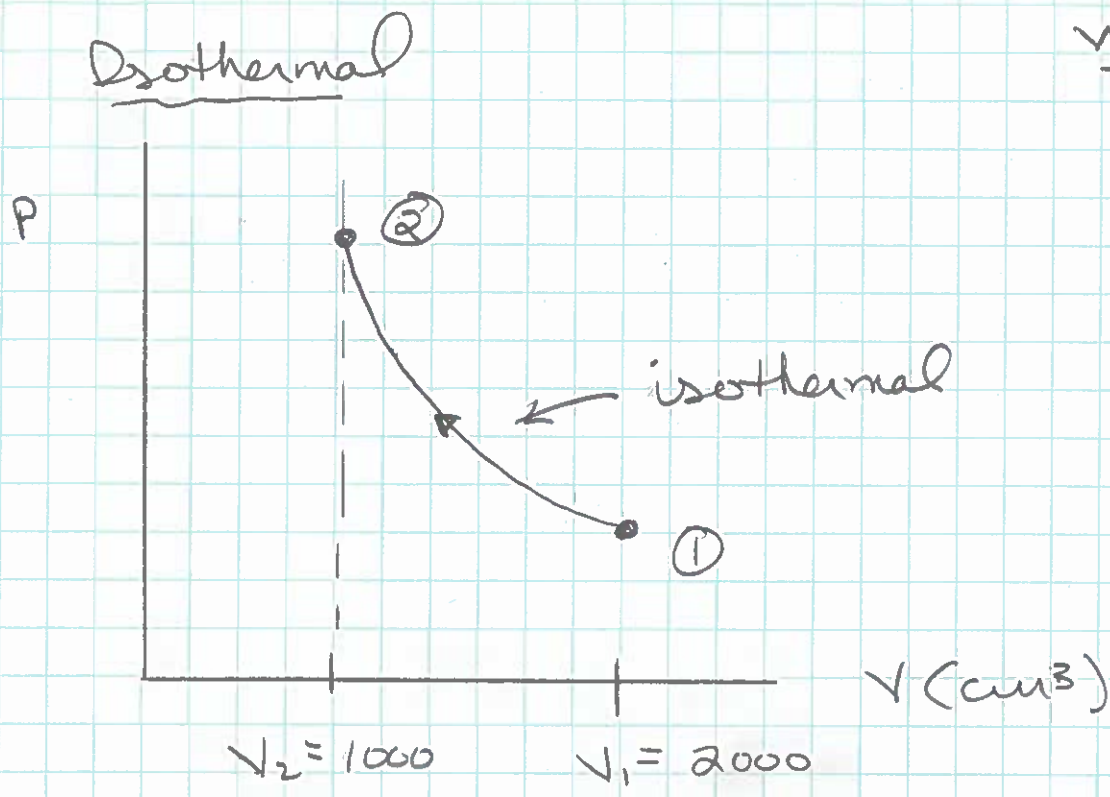
$$= -P_1 \int_{V_1}^{V_2} dV = -P_1 V \Big|_{V_1}^{V_2} = -P_1 (V_2 - V_1) = -P_1 \Delta V$$

Now, $PV = nRT \Rightarrow P_1 = \frac{nRT_1}{V_1}$

so

$$W_{1 \rightarrow 2} = -nRT_1 \left(\frac{V_2 - V_1}{V_1} \right) = +238 \text{ J}$$

c.)



d.) Isothermal, $T_2 = T_1$

$$W_{1 \rightarrow 2} = - \int_{V_1}^{V_2} p \, dV = -(\text{area under isothermal path.})$$

- Can p come outside the integral?
No, we need p as a function of V :

$$pV = nRT \Rightarrow p = \frac{nRT}{V}$$

So, integral is:

$$W_{1 \rightarrow 2} = - \int_{V_1}^{V_2} p \, dV = - \int_{V_1}^{V_2} \frac{nRT}{V} \, dV = -nRT_1 \int_{V_1}^{V_2} \frac{dV}{V}$$

So,

$$W_{1 \rightarrow 2} = -nRT_1 \ln V \Big|_{V_1}^{V_2} = -nRT_1 (\ln V_2 - \ln V_1)$$

$$\therefore \boxed{W_{1 \rightarrow 2} = -nRT_1 \ln \left(\frac{V_2}{V_1} \right) = +330 \text{ J}}$$

In the future, when we need to calculate the work for an isothermal process, we'll just use this equation.

But, you should go through the integration at least once.