



When switch is closed, current flows in the RC circuit that is time dependent. Assume that only that part of circuit nearest the loop produces a significant magnetic field. This time dependent field induces a current in the loop.

a.) When the switch closes at $t=0$:

$$I(t) = I_0 e^{-t/\tau} \quad \text{where } I_0 = \frac{\Delta V}{R_1} = 10\text{A}$$

$$\tau = RC = 1 \times 10^{-5}\text{s}$$

$I(t)$ is decreasing \Rightarrow flux is decreasing

and \vec{B}_{in} reinforces \vec{B} from $I(t)$

\therefore I_{in} is ccw

$$b.) \quad \mathcal{E} = \left| \frac{d\Phi_m}{dt} \right|$$

where:

$$\Phi_m = \int \vec{B} \cdot d\vec{A}$$

as we did in whiteboard Prob. WB 30-4

$$\Phi_m = \frac{\mu_0 I(t) l}{2\pi} \ln\left(\frac{r+w}{r}\right)$$

$$\text{and, } \frac{d\Phi_m}{dt} = \frac{\mu_0 l}{2\pi} \ln\left(\frac{r+w}{r}\right) \frac{dI(t)}{dt}$$

$$\text{where: } \frac{dI(t)}{dt} = I_0 \left(-\frac{1}{\tau}\right) e^{-t/\tau} = -\frac{I_0}{\tau} e^{-t/\tau}$$

$$\text{So: } I_{in} = \frac{\mathcal{E}}{R_2} = \frac{1}{R_2} \left| \frac{d\Phi_m}{dt} \right| = \frac{\mu_0 l}{2\pi R_2} \ln\left(\frac{r+w}{r}\right) \frac{I_0}{\tau} e^{-t/\tau}$$

$$\therefore I_{in} = 0.05345 \text{ A} = 53.45 \text{ mA}$$

for $t = 5 \text{ ms}$