

$$d\vec{B} = \frac{\mu_0}{4\pi} \frac{I d\vec{s} \times \hat{r}}{r^2}$$

For $d\vec{s}$ in either of the straight wire segments:

$$d\vec{s} \times \hat{r} = 0$$

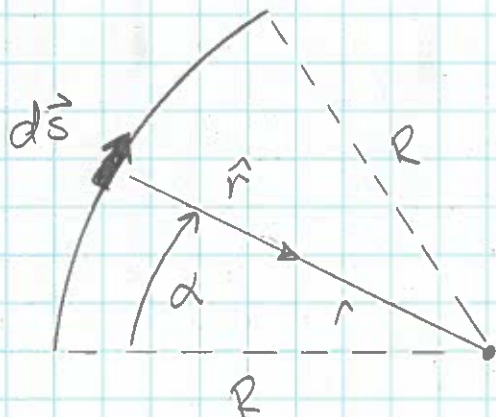
So, only the circular arc segment produces any field at P

For all $d\vec{s}$:

$$r = R$$

$$I d\vec{s} \times \hat{r} = I ds |\hat{r}| \sin 90^\circ = I ds$$

and, $ds = R d\alpha$



So:
$$dB = \frac{\mu_0}{4\pi} \frac{I R d\alpha}{R^2}$$

Direction: for all $d\vec{s}$, $d\vec{s} \times \hat{r}$ is into the page.

$$B = \int_{\text{wire}} dB = \frac{\mu_0 I}{4\pi R} \int_0^\theta d\alpha$$

$$= \frac{\mu_0 I}{4\pi R} \alpha \Big|_0^\theta \Rightarrow B = \frac{\mu_0 I \theta}{4\pi R}$$

Direction is into the page.