



$$dq = \lambda dx = \lambda_0 \frac{x}{L} dx$$

a.) Total charge, $Q = \int_{\text{Rod}} dq = \int_0^L \lambda_0 \frac{x}{L} dx$

So,

$$Q = \frac{\lambda_0}{L} \int_0^L x dx = \frac{\lambda_0}{L} \left(\frac{x^2}{2} \right) \Big|_0^L = \frac{\lambda_0}{L} \frac{L^2}{2}$$

So $\lambda_0 = \frac{2Q}{L}$

b.) dq produces a potential at P :

$$dV = \frac{k dq}{r} \quad dq = \lambda_0 \frac{x}{L} dx$$

So:

$$r = d + x$$

$$dV = \frac{k \lambda_0 \frac{x}{L} dx}{(d+x)} = \frac{k \lambda_0}{L} \frac{x dx}{(d+x)}$$

and

$$V = \int_{\text{Rod}} dV = \int_0^L \frac{k \lambda_0}{L} \frac{x dx}{(d+x)} = \frac{k \lambda_0}{L} \int_0^L \frac{x dx}{(d+x)}$$

$$V = \frac{K\lambda_0}{L} \int_0^L \frac{x dx}{(d+x)}$$

$$\frac{25-82}{2}$$

From Table: $\int \frac{x dx}{(a+x)} = x - a \ln(a+x)$

So:

$$V = \frac{K\lambda_0}{L} \left\{ x - d \ln(d+x) \right\} \Big|_0^L$$

$$= \frac{K\lambda_0}{L} \left\{ [L - d \ln(d+L)] - [-d \ln d] \right\}$$

$$= \frac{K\lambda_0}{L} \left\{ L + d [\ln d - \ln(d+L)] \right\}$$

$$= \frac{K\lambda_0}{L} \left\{ L + d \ln\left(\frac{d}{d+L}\right) \right\}$$

and $\lambda_0 = \frac{2Q}{L}$

So:

$$V = \frac{2KQ}{L^2} \left\{ L + d \ln\left(\frac{d}{d+L}\right) \right\}$$