



For physical pendulum and small angles:

$$\omega = \sqrt{\frac{Mgl}{I}}$$

l = distance from pivot to CM

where:

$$l = L/4$$

I = inertia about pivot point

$$I = I_{CM} + ML^2$$

and from table 12.2 $I_{CM} = \frac{1}{12} ML^2$

$$\text{So } I = \frac{1}{12} ML^2 + \frac{1}{16} ML^2 = \frac{7}{48} ML^2$$

and,

$$\omega = \sqrt{\frac{Mg(L/4)}{\frac{7}{48} ML^2}} = \sqrt{\frac{48g}{28L}} = \sqrt{\frac{12g}{7L}}$$

$$\therefore f = \frac{\omega}{2\pi} = \frac{1}{2\pi} \sqrt{\frac{12g}{7L}}$$