



2D Trajectory

1 → 2:

$$x_1 = 0$$

$$v_{1x} = v_1$$

$$v_{1y} = 0$$

$$a_y = -g$$

$$a_x = 0$$

$$x_2 = d$$

$$y_2 = 0$$

$$y_1 = h$$

y-motion:

$$y_2 = y_1 + v_{1y} \Delta t + \frac{1}{2} a_y \Delta t^2 \quad \Delta t = t_1 - \frac{t_0}{2}$$

$$0 = h - \frac{1}{2} g t_1^2$$

$$t_1 = \sqrt{\frac{2h}{g}}$$

x-motion:

$$x_1 = x_0 + v_{1x} \Delta t + \frac{1}{2} a_x \Delta t^2$$

$$d = v_1 t_1 = v_1 \sqrt{\frac{2h}{g}}$$

$$\text{So: } v_1 = d \sqrt{\frac{g}{2h}}$$

Conserve momentum 0 → 1:

$$\text{x-comp: } m v_b = (m+M) v_1$$

$$\text{So } v_b = \frac{m+M}{m} v_1 = \frac{m+M}{m} d \sqrt{\frac{g}{2h}}$$