

$m =$ mass of child + sled.

Conserve energy $i \rightarrow f$:

$$\Delta E_{\text{mech}} = \Delta K + \Delta U = W_{\text{nc}}$$

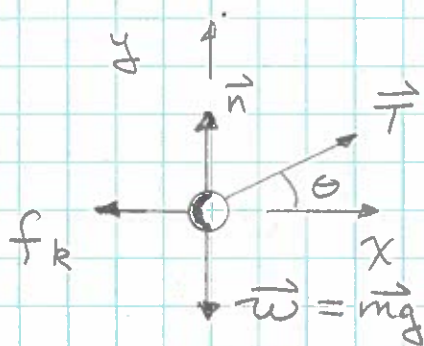
$$\frac{1}{2} m (v_f^2 - v_i^2) = W_T + W_{\text{fric}}$$

Now:

$$W_T = \vec{T} \cdot \Delta \vec{r} = Td \cos \theta$$

and for friction:

FBD:



$$\sum F_y = T \sin \theta + n - w = ma_y = 0$$

So:

$$n = mg - T \sin \theta$$

and,

$$f_k = \mu_k n$$

$$f_k = \mu_k (mg - T \sin \theta)$$

and

$$W_{\text{fric}} = \vec{f}_k \cdot \Delta \vec{r} = f_k d \cos 180^\circ = -f_k d$$

$$= -\mu_k d (mg - T \sin \theta)$$

∴ energy equiv'n is:

$$\frac{1}{2} m v_f^2 = Td \cos \theta - \mu_k d (mg - T \sin \theta)$$

$$\text{Or, } v_f = \sqrt{\frac{2d}{m} \{ T \cos \theta - \mu_k (mg - T \sin \theta) \}}$$