



a.) First find maximum speed at 2 to just stay on the track:

at 2: FBD



$$\Sigma F_r = -w - n = ma_r = \frac{mv^2}{r}$$

When car just leaves track, $n \rightarrow 0$, so

$$mg = \frac{mv^2}{R} \Rightarrow v_2 = \sqrt{gR}$$

Now, conserve energy $0 \rightarrow 2$:

$$\Delta E_{\text{mech}} = \Delta K + \Delta U_g = 0$$

$$\frac{1}{2} m (v_2^2 - v_0^2) + mg(y_2 - y_0) = 0$$

$$\frac{1}{2} v_2^2 + g(R - h) = 0$$

From above, $v_2^2 = gR$

$$\frac{1}{2} gR + gR - gh = 0$$

$$\therefore \underline{h = \frac{3}{2} R}$$

b.) Here's a better part b:

"What is the apparent weight felt by the rider at the bottom of the first loop (point 1)?"

Find speed at 1: Conserve energy $0 \rightarrow 1$:

$$\Delta E_{\text{mech}} = \Delta K + \Delta U_g = 0$$

$$\frac{1}{2} m (v_1^2 - v_0^2) + mg(y_1 - y_0) = 0$$

$$\frac{1}{2} v_1^2 - gh = 0$$

$$\therefore v_1 = \sqrt{2gh}$$

Now, at 1, FBD:



$$\Sigma F_r = n - w = ma_r = \frac{mv^2}{r}$$

"apparent weight" = n

$$\text{So, } n = \frac{mv_1^2}{R} + mg$$

$$\text{from above, } v_1^2 = 2gh$$

$$\text{and from part a, } h = \frac{3}{2}R$$

So,

$$n = \frac{m}{R} 2g \left(\frac{3}{2}R \right) + mg$$

$$= 3mg + mg$$

$$= 4mg$$

$$\therefore \underline{n = w_{\text{app}} = 4w}$$